

A (Very) Brief Survey of Compiler Design

Independent Study
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Objective

```
fn main() {  
    println!("Hello, world");  
}
```



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Materials

Source: Modern Compiler Implementation in Java, by Andrew W. Appel and Jens Palsberg

Frontend

- Lexical Analysis
- Parsing
- Abstract Syntax Trees
- Semantic Analysis
- IR

Backend

- Activation Records
- Blocks
- Traces
- Liveness Analysis
- Register Allocation

Focus

Frontend

- Lexical Analysis
- Parsing
- Abstract Syntax Trees
- Semantic Analysis
- IR

Backend

- Activation Records
- Blocks
- Traces
- Liveness Analysis
- Register Allocation

Lexical Analysis

Lexical Tokens

```
fn main() {  
    println!("Hello, world");  
}
```

123

// comments

fn

main

(

)

{

println

!

(

"Hello, world"

)

;

}

Regular Expressions

Represent sets of strings

Symbol, Alternation, Concatenation, Epsilon, Repetition (Kleene closure)

$(0 \mid 1)^* \cdot 0$

Kleene closure: For some regular expression, M , its Kleene closure is M^* , the concatenation of zero or more strings in M

Even Binary Numbers

00000010	(4)
10000000	(128)



Sequence of zero or
more "0"s and "1"s in
any combination

Concatenate this
sequence with a single
0

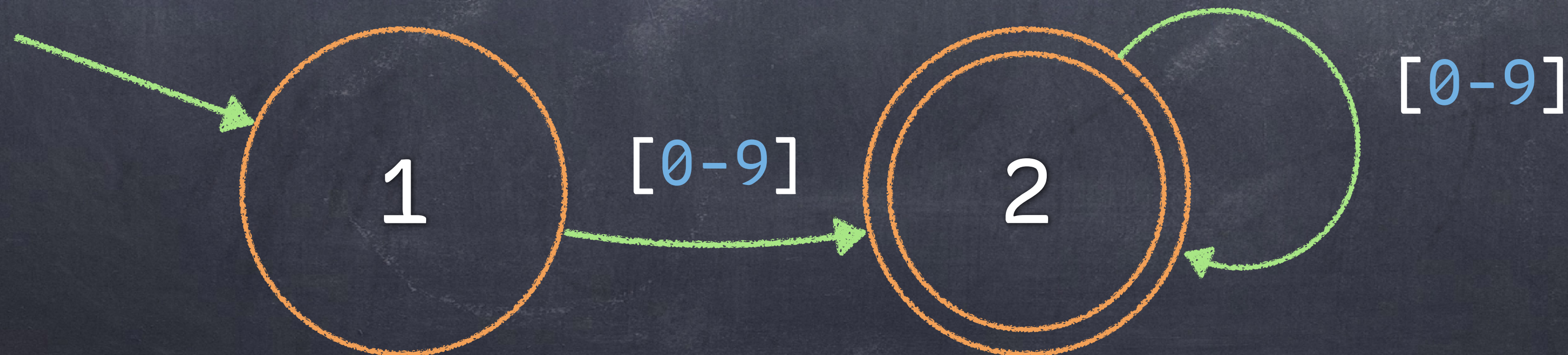
Finite Automata

A way to formalize regular expressions so they can be implemented by a computer

Consist of **states**, **edges**, and **symbols**

$[0-9]^+$

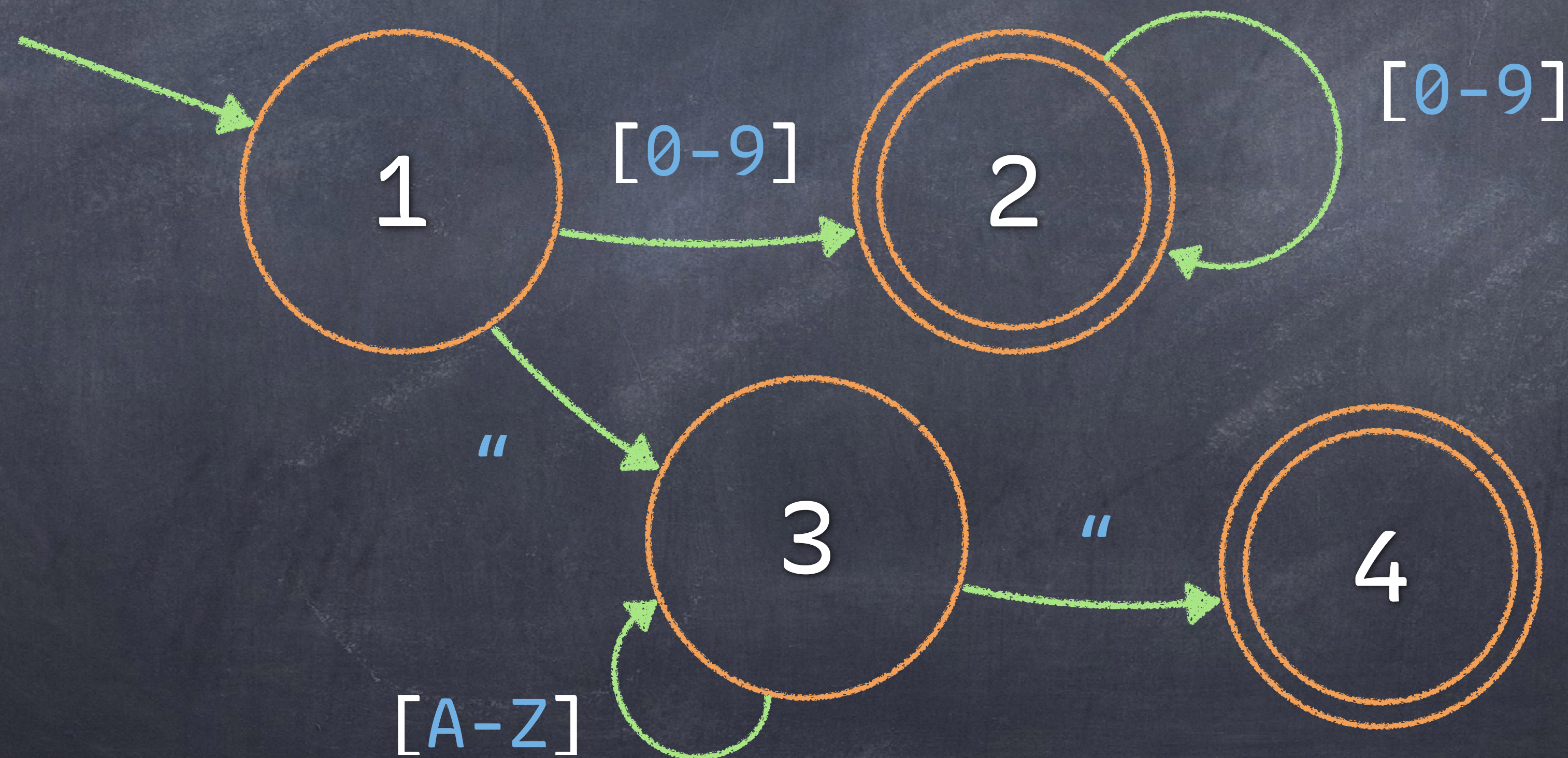
(+ denotes repetition of one or more times)



Deterministic Finite Automata

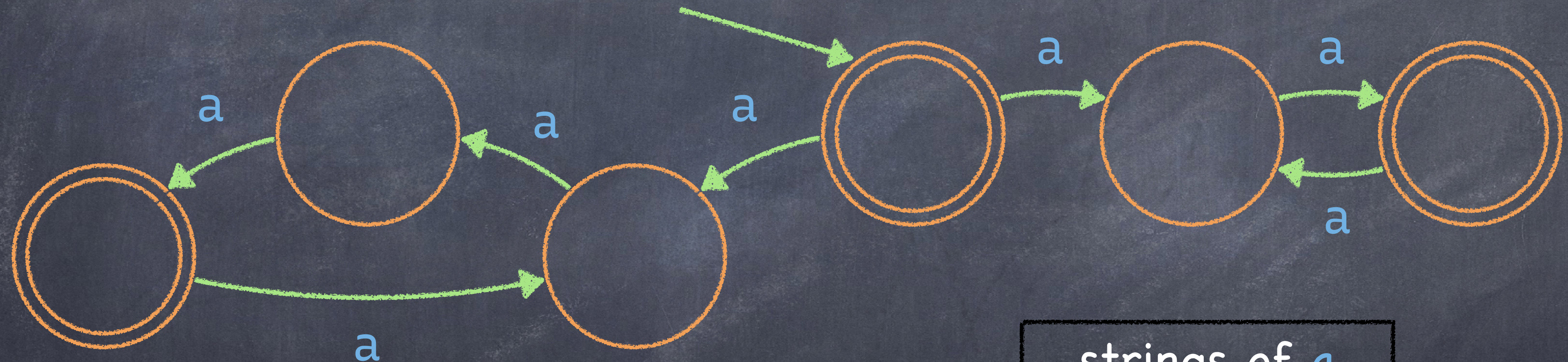
We can combine automata to create a lexical analyzer

The goal is to find the longest match; i.e. the longest substring of the input that is a valid token



Nondeterministic Finite Automata

An automata which has a choice of edges labeled with the same symbol to flow from the current state



strings of a
whose length is
a multiple of 3

strings of a
whose length is
even

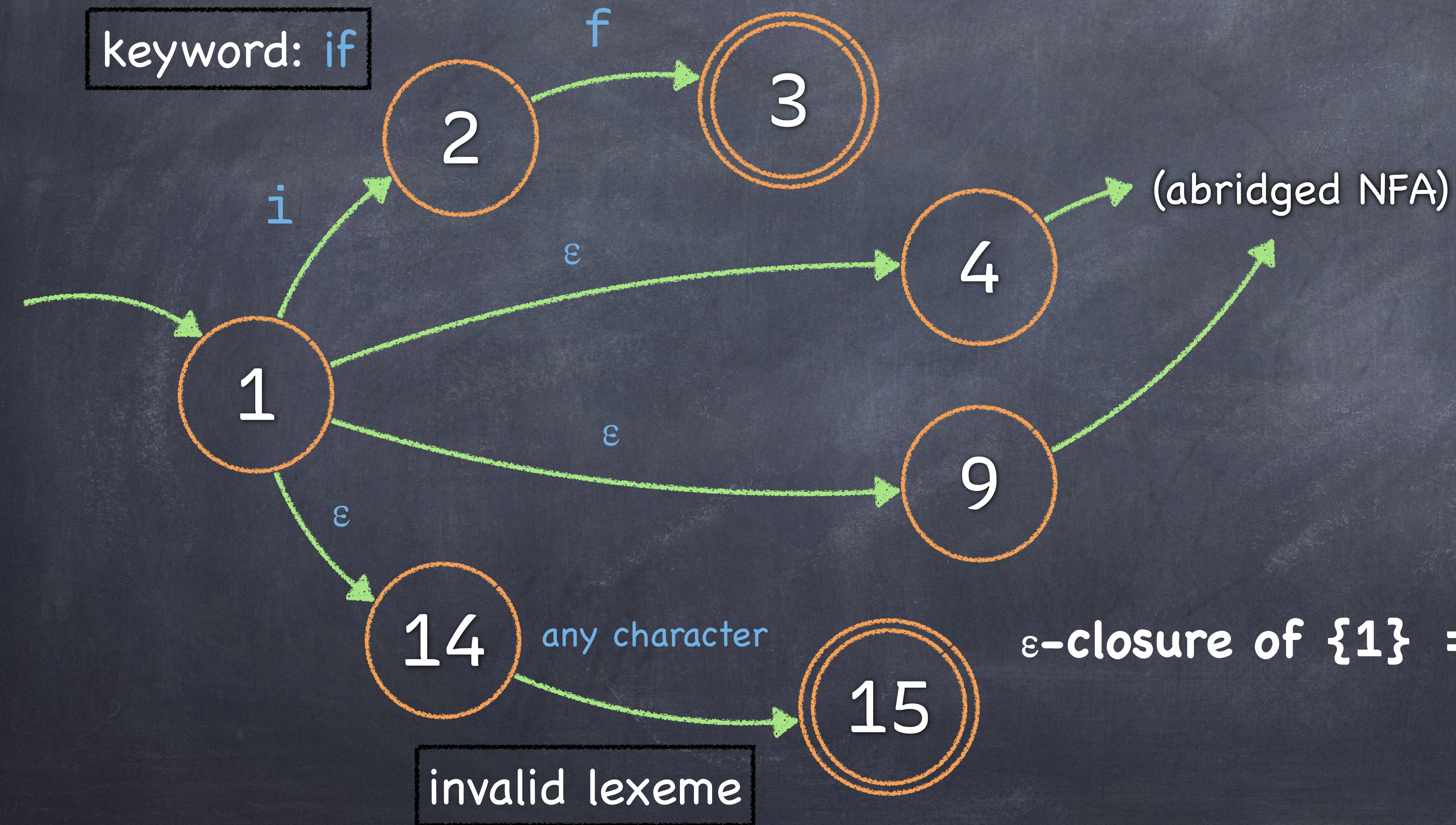
So what?

We can convert regular expressions to nondeterministic finite automata,
and then to deterministic finite automata

- Simultaneously traverse all possibilities at each “step” of the NFA
- Each set of destination states for these possibilities is called the ϵ -closure
- Every ϵ -closure is one node in the corresponding DFA

Partial Example

keyword: if



ϵ -closure of $\{1\} = \{1, 4, 9, 14\}$

ϵ -closure of $\{1\}$

$\{1, 4, 9, 14\}$

states reachable without
consuming a token of the
input

ϵ -closure always contains
itself

Parsing

Context-Free Grammars

Describes a language using sets of **productions**

Each production follows the form:

$\text{symbol} \rightarrow s_1 s_2 s_3 \dots s_n$

Terminal

"Hello, world"

123

println

Nonterminal

expression

function

An Example Grammar

5 * 6 / (3 + 3)

expression $\rightarrow$ term;

term $\rightarrow$ factor (("+" | "−") factor)*;

factor $\rightarrow$ primary (("∗" | "/") primary)*;

primary $\rightarrow$ [0-9]+ | "(" expression ")";

expression → term;

term → factor (("+" | "-") factor)*;

factor → primary (("*" | "/") primary)*;

primary → [0-9]+ | "(" expression ")";

Predictive Parsing

Recursive Descent

5 * 6 / (3 + 3)

primary * 6 / (3 + 3)

primary * primary / (3 + 3)

primary * primary / (primary + primary)

primary * primary / (term)

primary * primary / primary

factor

expression

Predictive Parsing

Limitations

Cannot parse grammars that use **left recursion** or when two productions for the **same nonterminal** start with the same symbols

$$E \rightarrow E \text{ "+" } T;$$
$$E \rightarrow T;$$
$$S \rightarrow \text{"if"} E \text{"then"} S \text{"else"} S;$$
$$S \rightarrow \text{"if"} E \text{"then"} S;$$

Eliminating Left Recursion

$$E \rightarrow E \text{ "+" num};$$
$$E \rightarrow \text{num};$$

Rewrite using right recursion

$$E \rightarrow \text{num } E';$$
$$E' \rightarrow \text{"+" num } E';$$
$$E' \rightarrow ;$$

Left Factoring

$S \rightarrow \text{"if"} E \text{"then"} S \text{"else"} S;$

$S \rightarrow \text{"if"} E \text{"then"} S;$

Create another nonterminal, X

$S \rightarrow \text{"if"} E \text{"then"} S X;$

$X \rightarrow \text{"else"} S;$

$X \rightarrow ;$

LR Parsing

Left-to-right parse with a rightmost-derivation

Shift and **reduce** are the primary actions

Has a **stack** and an **input**

Shift: Advance the input one token and push that token onto the stack

Reduce: Pop the stack as many times as the number of symbols on the right-hand side of a production rule

LR Parsing

A deterministic finite automata is applied to the **stack** to determine when to **shift** and when to **reduce**

The edges of the DFA are labeled by the symbols that can appear on the **stack**

The transitions between edges can be modeled by a simple table

(1) $S \rightarrow S \text{ ";"}$

(2) $S \rightarrow id \text{ " := " } E;$

..

(5) $E \rightarrow num$

Parse Table

	id	num	;	:=		S	E
1	s4					g2	
4				s6			
6	s20	s10					g11
10			r5				
11			r2				

Based on DFA: numbers represent DFA state numbers

Stack

Input

Action

a := 7; shift

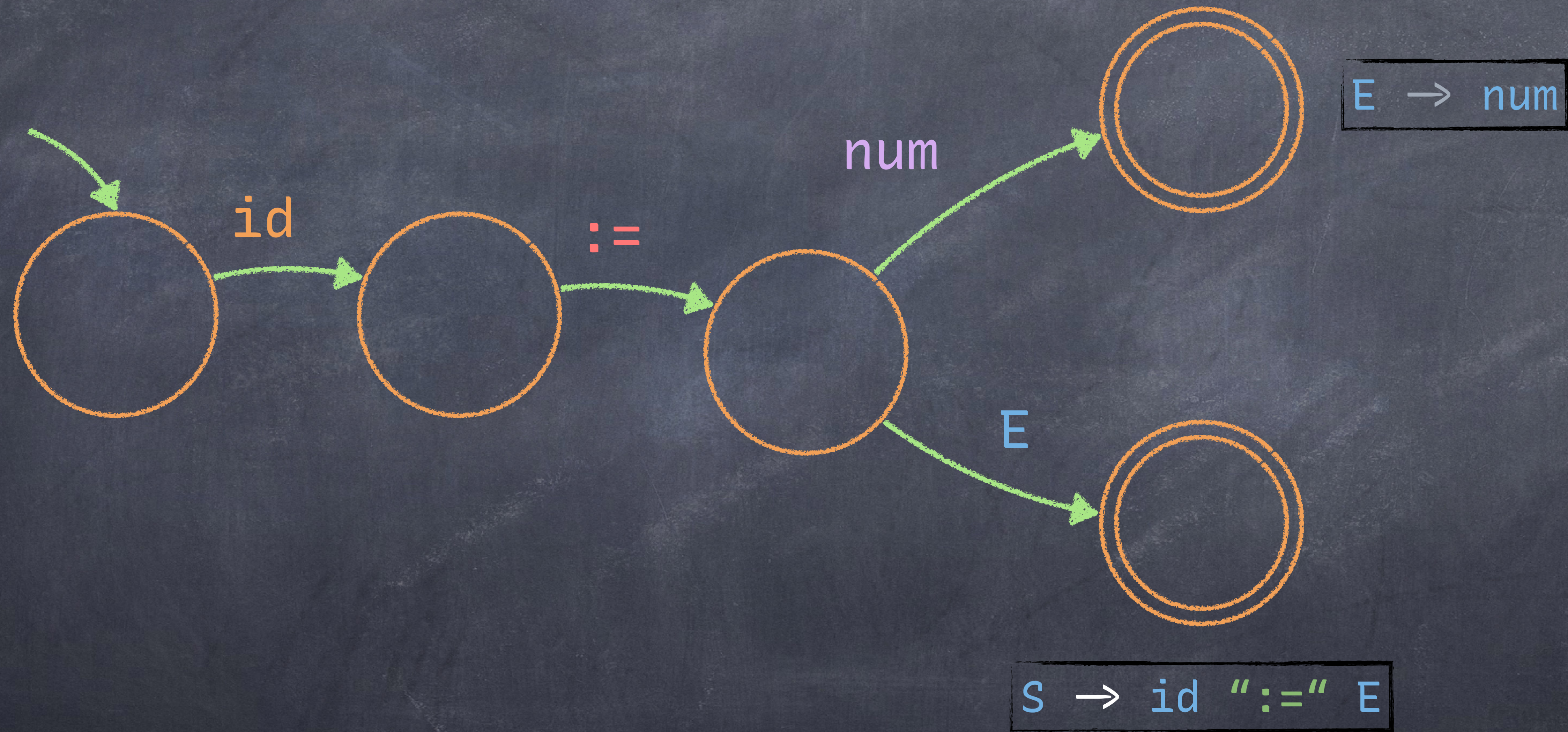
id := 7; shift

id := 7; shift

id := num; reduce $E \rightarrow num$

id := E; reduce $S \rightarrow id \text{ " := " } E$

DFA: Stack



Interlude

Now what?

During parsing, we convert the lexemes to an
Abstract Syntax Tree (AST)

Each nonterminal of a grammar corresponds to a
node type

Using this tree we can more easily perform:

- Type checking
- Translation to an
intermediate
representation

A (re)Introduction to Visitors

Incredibly useful for many semantic analysis phases, including type checking

Each AST node type implements two methods:

- `accept()`
- `visit()`

i.e. type checking:

```
left.accept(this).type == right.accept(this).type
```

Intermediate Representation (IR)

A machine-independent abstraction for assembly

Simplifies the process for converting the recursive
AST into a more machine-friendly format

Examples of IR nodes:

MOVE(src, dest) JUMP(label) CJUMP(trueLabel, falseLabel)
BINARY(op, left, right) SEQ(left, right) TEMP(name)
ESEQ(stmt, exp)

ESEQ?

ESEQ(stmt, exp)

Execute stmt, then evaluate and return exp

```
def id(x):  
    return x  
  
y = id(5 + 5)
```



```
MOVE(t2, ESEQ(MOVE(t1, CALL(BINARY(Add,  
5 + 5))))), t1))
```

Wait, this violates assembly's linearity!

Simplifies translation to IR, can clean it up later

Eliminating ESEQ

Recursively pull all ESEQ nodes out of the tree

Replace ESEQ node with its expression

```
MOVE(t2, ESEQ(MOVE(t1, CALL(BINARY(Add,  
5 + 5))), t1))
```



```
MOVE(t1, CALL(BINARY(Add, 5 + 5)))  
  
MOVE(t2, t1)
```

Instruction Selection

For each IR node, we recursively generate assembly instructions, starting with the most deeply nested

```
MOVE(t1, CALL(BINARY(Add, 5 + 5)))
```

```
MOVE(t2, t1)
```

```
mov t1, 5
```

```
mov t2, 51
```

```
add t1, t2
```

```
mov t1, %rdi
```

```
call
```

```
mov %rax, t1
```

```
mov t1, t2
```

¹ extra move instructions can be cleaned up by register allocator

Blocks and Traces

What about control flow?

We convert the linear list of statements into a set of **blocks**, and then arrange those **blocks** into **traces**

Blocks are always **entered** at the beginning and **exited** at the end

Traces are used to optimize control flow (more details on this later)

Blocks

A **block** is a sequence of statements where:

- The first statement is a **LABEL**
- The last statement is either a **JUMP** or **CJUMP**
- Each of these must occur at most one time

Generating Blocks

Starting with the first statement, when a **LABEL** is found, start a new block

Whenever a **JUMP** or **CJUMP** is found, the current block is ended

If any block does not end with a **JUMP** or **CJUMP**, add a **JUMP** to the next block's label

If any block has no **LABEL**, create a new one for it

Example

Color-coded blocks

```
.main:  
  
mov t1,5  
  
mov t2,6  
  
jmp .L1 if t1 < t2 else .L2
```

```
.L1  
  
add t1,t2  
  
jmp .L3
```

```
.L2  
  
sub t1,t2  
  
jmp .L3
```

```
.L3  
  
call printf t1  
  
jmp main.epilogue
```

```
1  def main():  
2      t1 = 5  
3      t2 = 6  
4      if t1 < t2:  
5          t1 += t2  
6      else:  
7          t1 -= t2  
8      print(t1)
```

How do we order these?

Generating Traces

Start with some initial block, and follow a possible execution path (the rest of the trace)

Repeat until all blocks are associated with one trace

For any blocks which end with an unconditional jump and are followed by the target label, remove the jump

Add all blocks to a list, Q

while Q is not empty:

 Start a new trace, T

 Remove the head element b from Q

 while b is not marked:

 Mark b

 Append b to the end of T

 for successor of b:

 if successor is not marked:

 b = c

 End T

Example Traces

```
.main:  
  
mov t1,5  
  
mov t2,6  
  
jmp .L1 if t1 < t2 else .L2
```

Trace #1

.L3

call printf t1

jmp main.epilogue

.L2

sub t1,t2

jmp .L3

Trace #2

.L1

add t1,t2

jmp .L3

```
1 def main():  
2     t1 = 5  
3     t2 = 6  
4     if t1 < t2:  
5         t1 += t2  
6     else:  
7         t1 -= t2  
8     print(t1)
```

Liveness Analysis

What is liveness?

For a given variable, it is live if its current value will be used in the future

We can calculate the **live range** of a particular variable by starting at a **use** of a variable and searching backwards until that variable is **defined**

This can be done either **one-variable-at-a-time** or using set equations

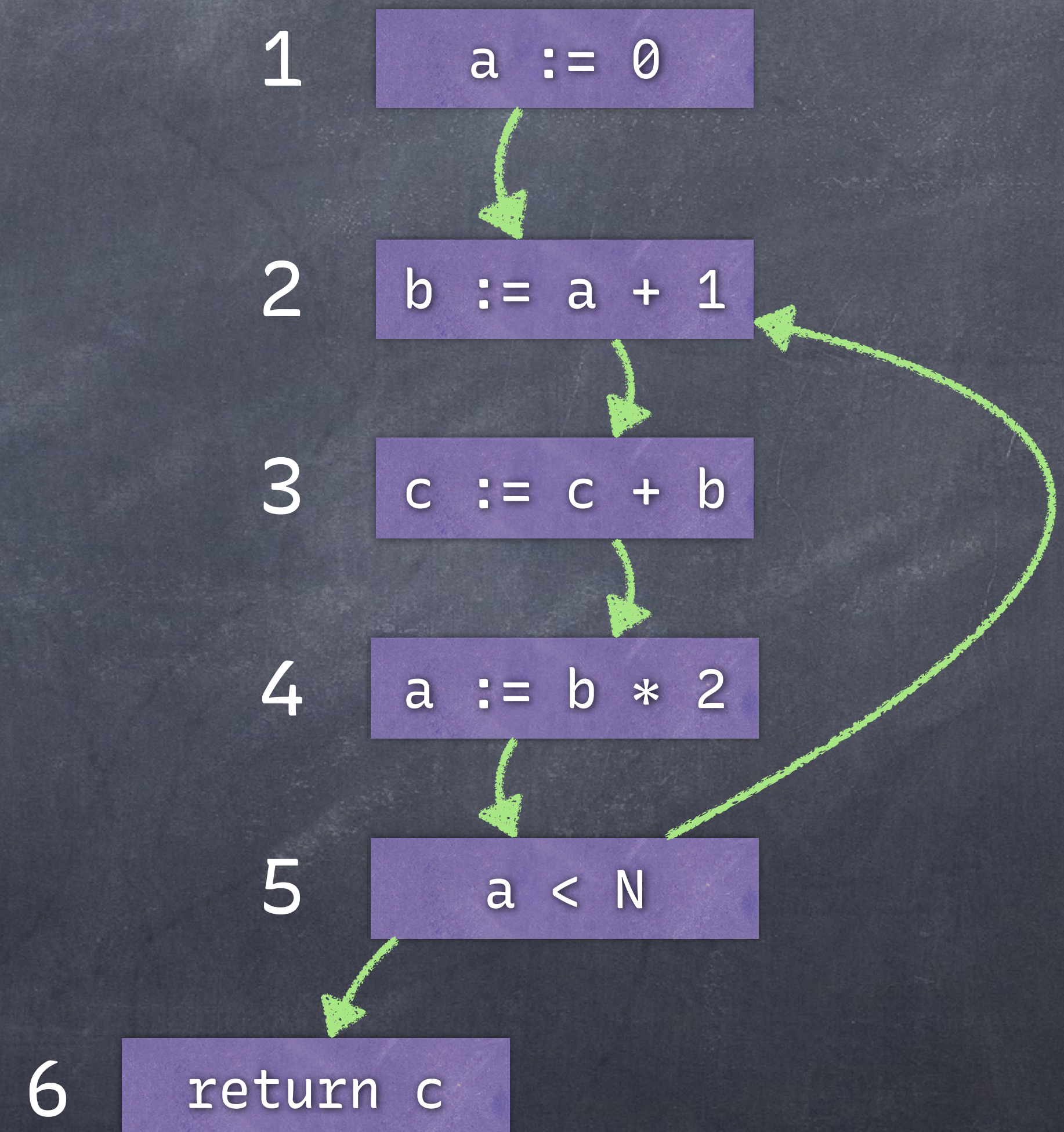
Example

$a = \{1 \rightarrow 2, 4 \rightarrow 5, 5 \rightarrow 2\}$

$b = \{2 \rightarrow 3, 3 \rightarrow 4\}$

$c = \text{entire range}$

$n \rightarrow m$ is $(n, m]$



Interference Graphs

	a	b	c
a			x
b			x
c	x	x	

How are control flow graphs created?

Based on breadth-first search

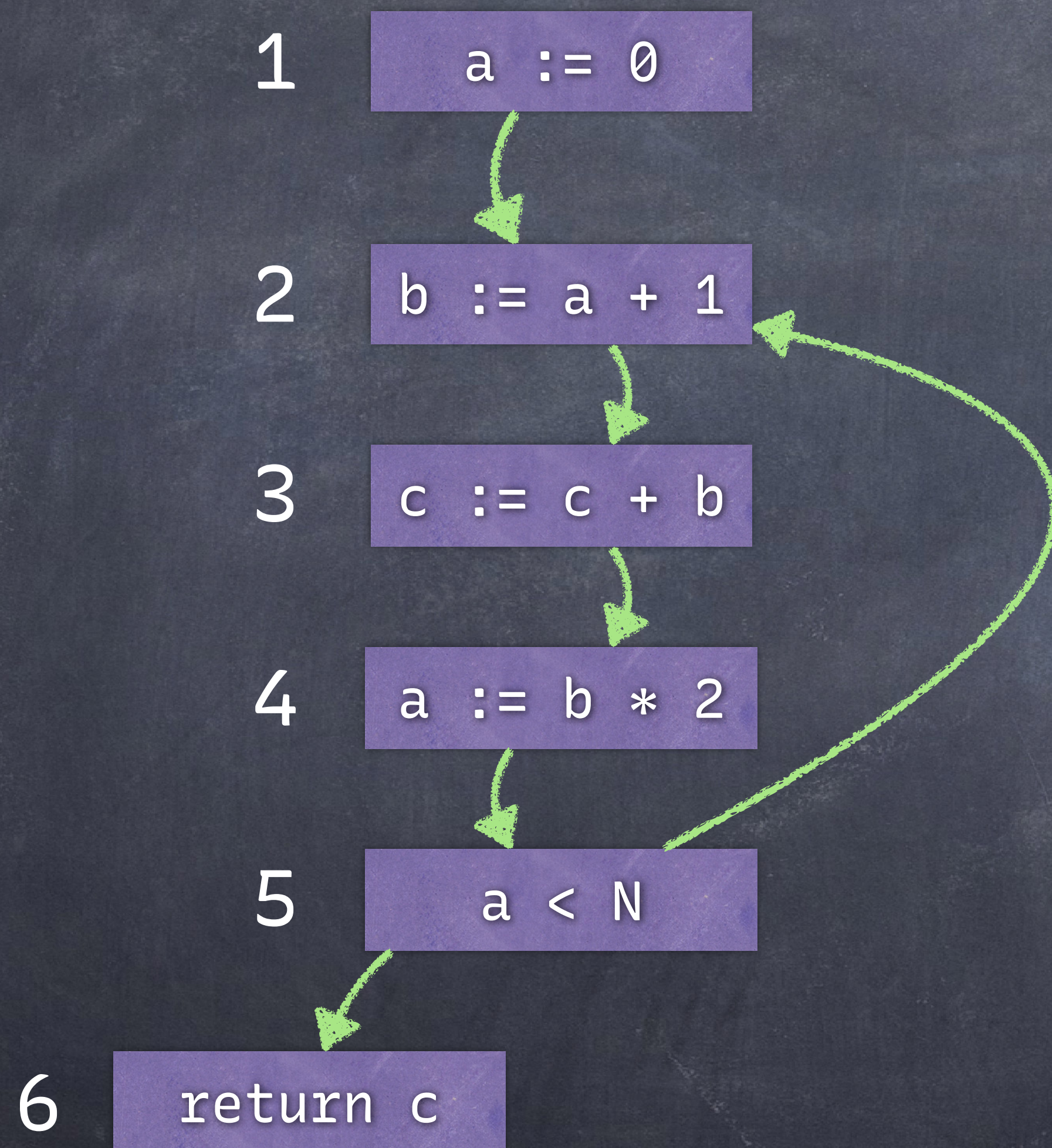
Start with a queue containing the index of the first statement

For each statement, its "neighbors" are any successor nodes

Add an edge between statement and each neighbor

Add neighbors to queue

Example Revisited



(5) is the only interesting node

Has two successors: 6 and 2

Project Challenges

Tooling Pitfalls

There are various ways to automate lexical analysis and parsing for both LL(k) and LR(k) classes of grammars

Examples

JavaCC

SableCC (Java)

pest (Rust)

Type-Checking

```
foo.bar.baz = 5;
```

Figure out whether bar exists on foo and what its type is

Now that we know what bar's type is, see if baz exists, etc.

Straightforward concept, several small errors and many cases to handle

What if bar is a function?

Repetitive Analysis

```
foo.bar.baz = 5;
```

It's useful to know what these types are in future phases

We don't want to recompute every time

Initially was not saving results of type-checking phase which complicated future phases

How do we eliminate abstractions?

High-level concepts difficult to translate to
something compilable

Classes or structs may have nested fields, but stack
frames are linear

Solution: flatten structs

ESEQ and its myriad issues

Unresolved Questions:

Scope of Program Input

What is the class of valid programs?

Where are the edge cases?

How do I adequately test algorithms on **many** different inputs?

Thanks for listening